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Spatial coherence measurement

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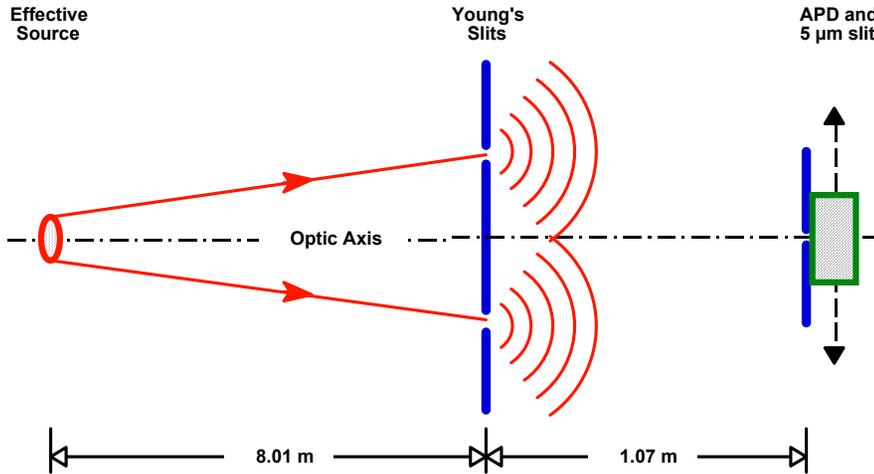


Motivation

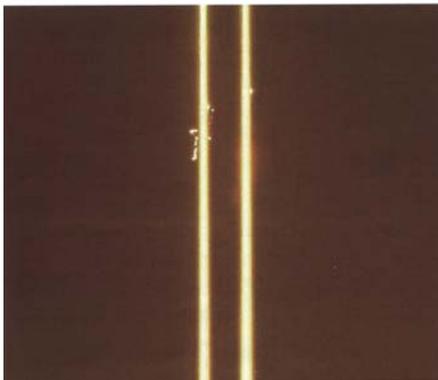
- **Unique coherence-based experiments relating to holography, microfocussing and phase measurement**
- **Third generation synchrotrons produce very bright, partially coherent X-rays**
- **Fourth generation sources, pulsed sources**
- **Characterisation of spatial coherence is a high priority**
- **Coherence “degradation” by beamline optics?**
- **Aim: develop theoretical and experimental program to measure the spatial coherence and phase properties of radiation**
- **=> Cohereometer**



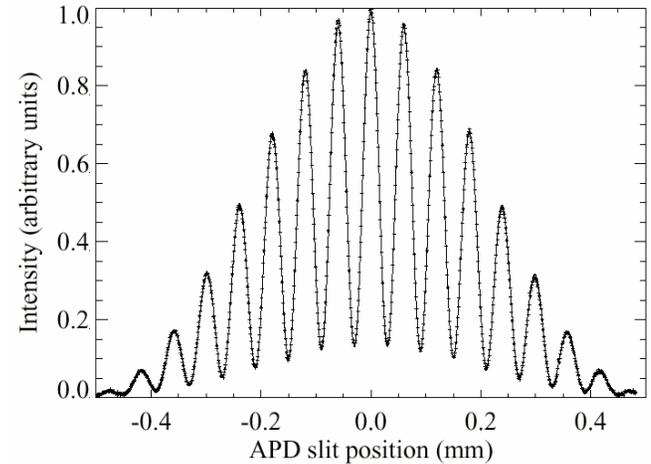
Young's experiment (1.1 keV)



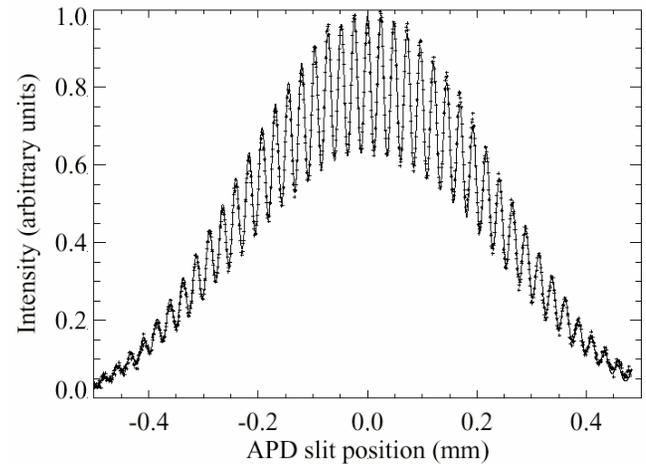
Experiment geometry (top view)



Young's slits (1.6 μm Au, 3 μm wide, 10 μm apart)



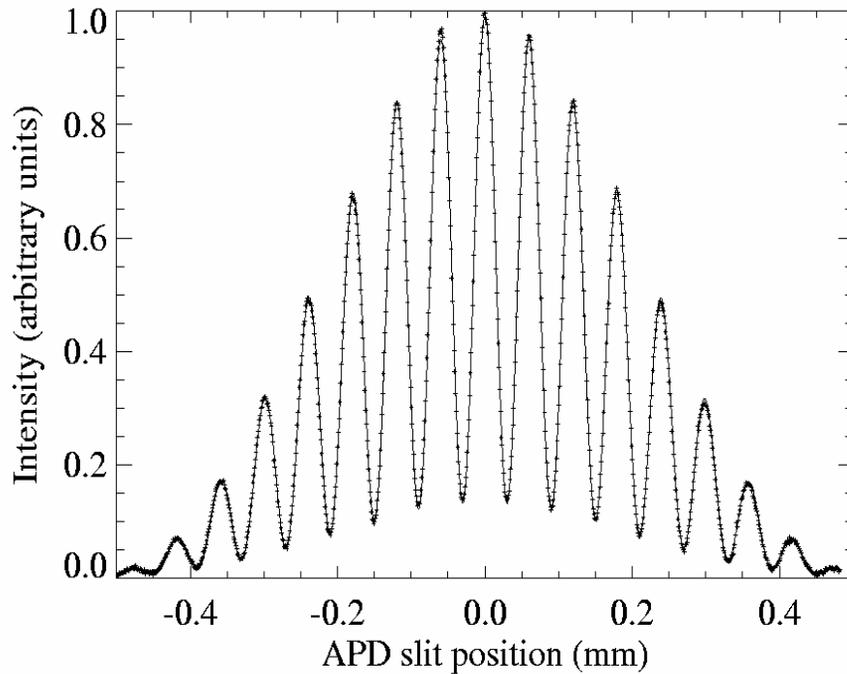
20 μm slit separation



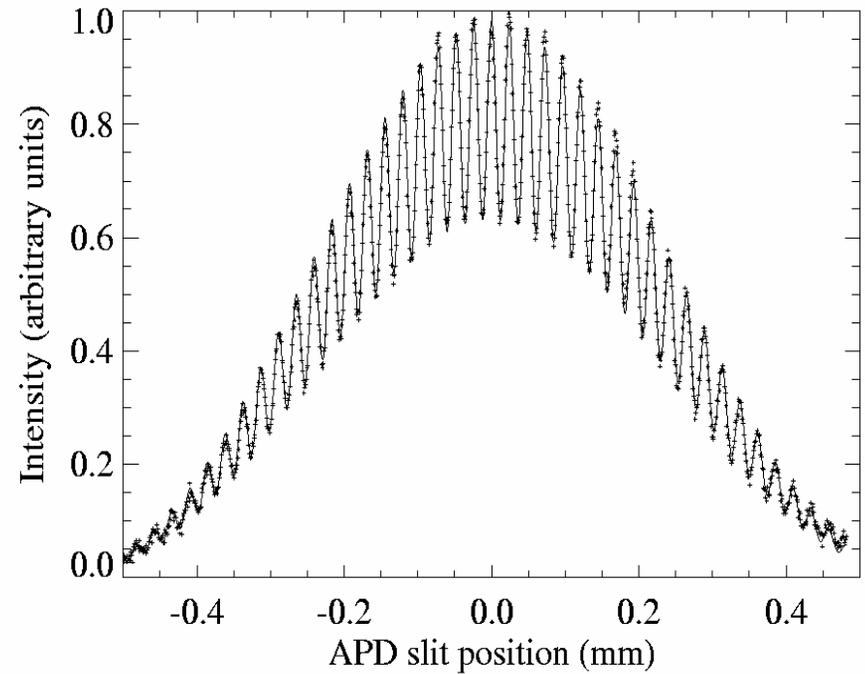
50 μm slit separation

Diffraction profiles and fitting

- Energy 1.1 keV
- + data — fit to data



Young's slit separation = 20 μm



Young's slit separation = 50 μm

$$|\mu_{12}| = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$$

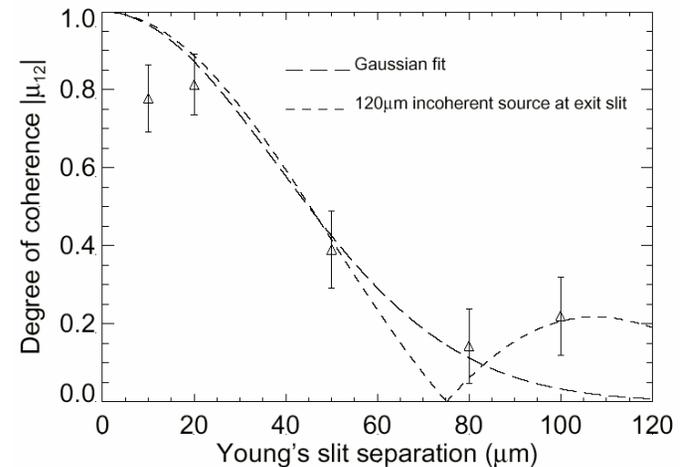
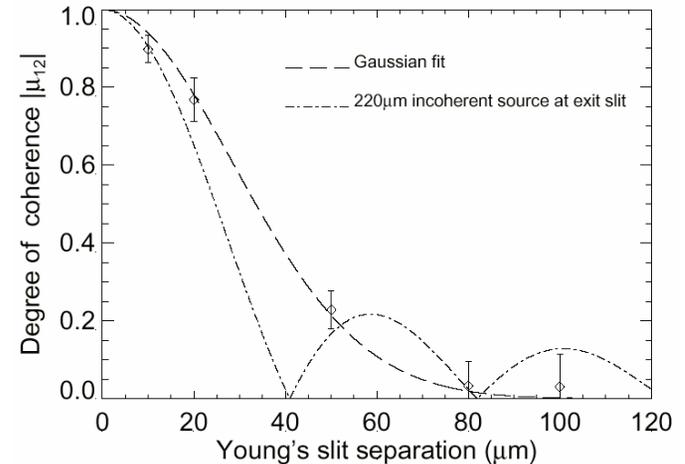
Coherence function at beamline 2-ID-B

Horizontal degree of spatial coherence $|\mu_{12}|$
measured 8 m from monochromator exit slit.
 $|\mu_{12}|$ is dominated by beamline optics

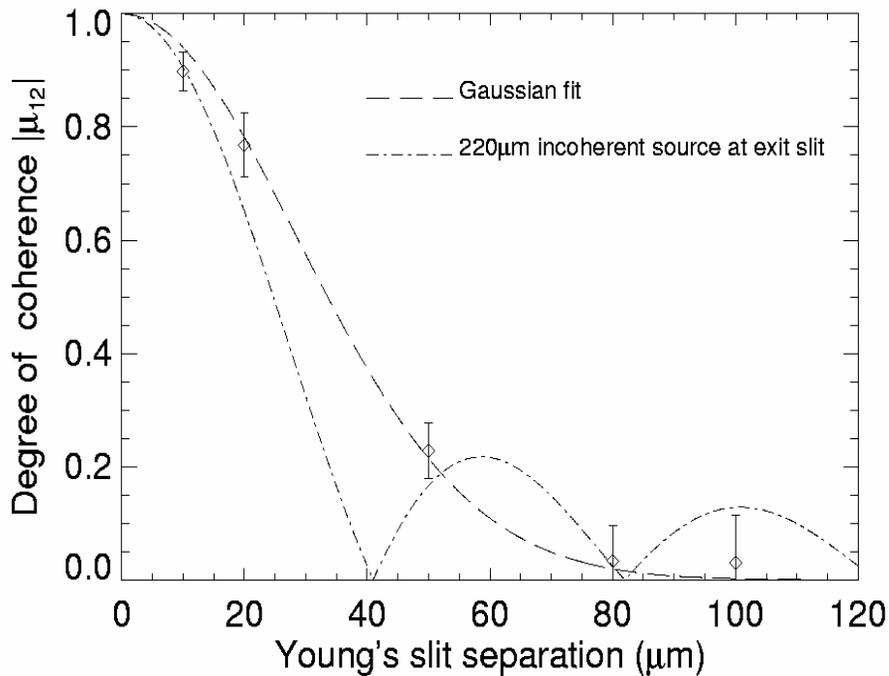
Energy = 1.1 keV
Entrance slit = 50 μm
Exit slit = 220 μm

$$W_C = \left(W_{\text{slit}}^2 + W_{\text{source}}^2 \right)^{\frac{1}{2}}$$

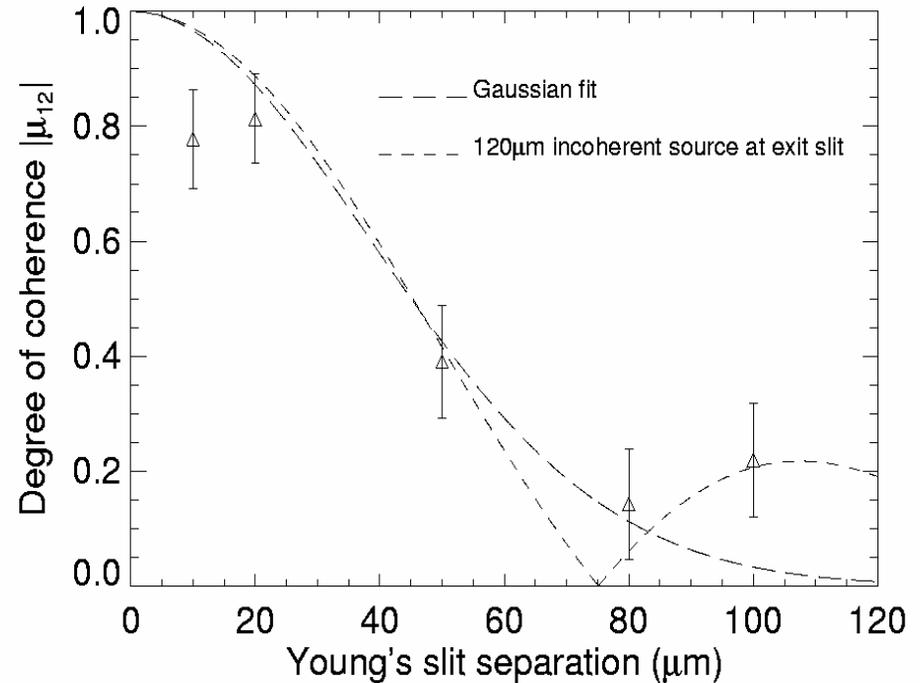
$|\mu_{12}|$ measured with 120 μm exit slit. $|\mu_{12}|$ is
dominated by exit slit, producing sinc profile



Coherence function dependence on exit slit



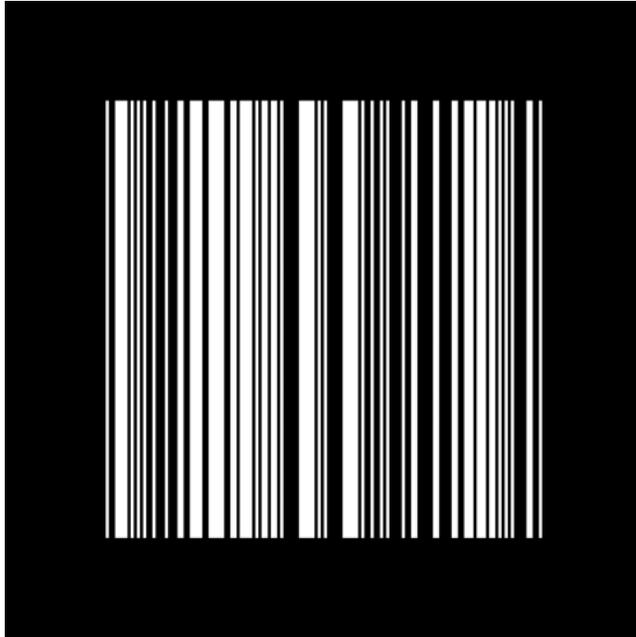
Exit slit at 200 μm
 Gaussian profile



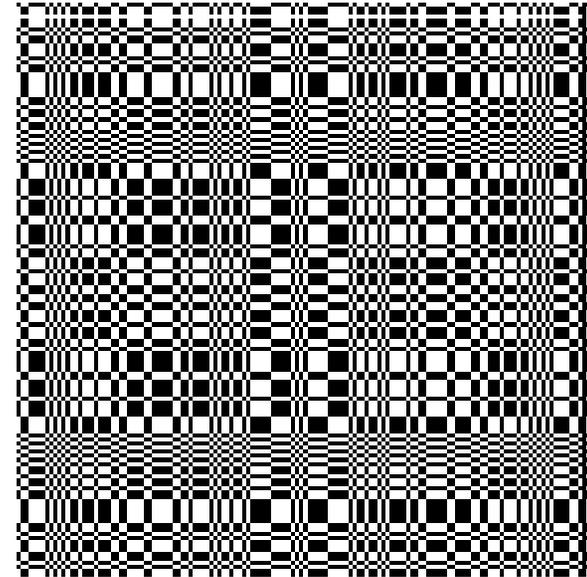
Exit slit at 100 μm
 Sinc profile

$$\mu_{12} = \frac{\sin\left(\frac{\pi\sigma\Delta}{\lambda z'}\right)}{\frac{\pi\sigma\Delta}{\lambda z'}}$$

Parallel measurement: Uniformly Redundant Arrays



1D



2D

- All possible aperture separations occur with same frequency
- 1D URA equivalent to many simultaneous Young's experiments

Experiments at APS

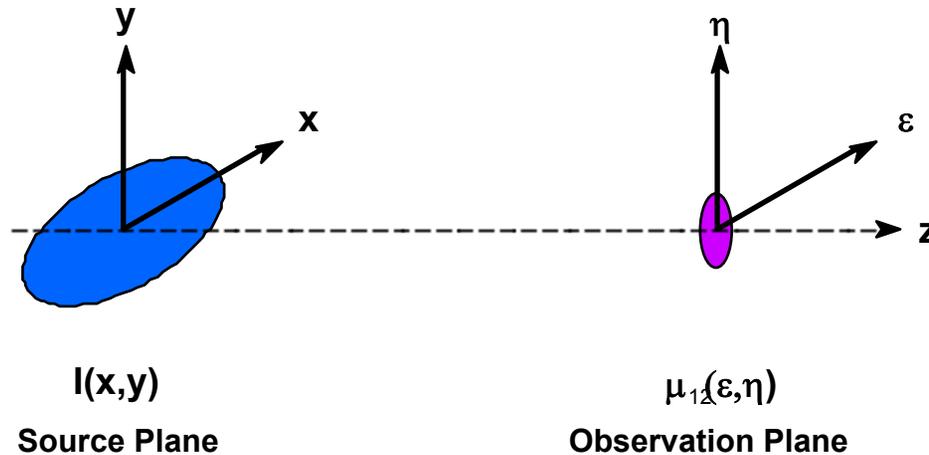
- Fast measurement of 1D and 2D coherence functions with URAs and CCDs (< 1 min exposures)
- Performed at APS 2-ID-B (soft) and 2-ID-D (hard x-ray) beamlines
- Measured with 8, 2.5 nm-rad electron beam emittance
- Obtain $|\mu_{12}|$ by Fresnel inversion



1D URA (1.18 μm Au, 2.5 μm min. width)



Coherent field from incoherent source



van Cittert-Zernike theorem

$$\mu_{12}(\varepsilon, \eta) = e^{i\phi} \frac{\int I(x, y) e^{-ik(x\varepsilon + y\eta)/z} dx dy}{\int I(x, y) dx dy}$$

Fourier-invert to obtain source size
and shape (assumes symmetry)

$$I(x, y) \propto FT^{-1} \{ \mu_{12} \}$$

Partially coherent field

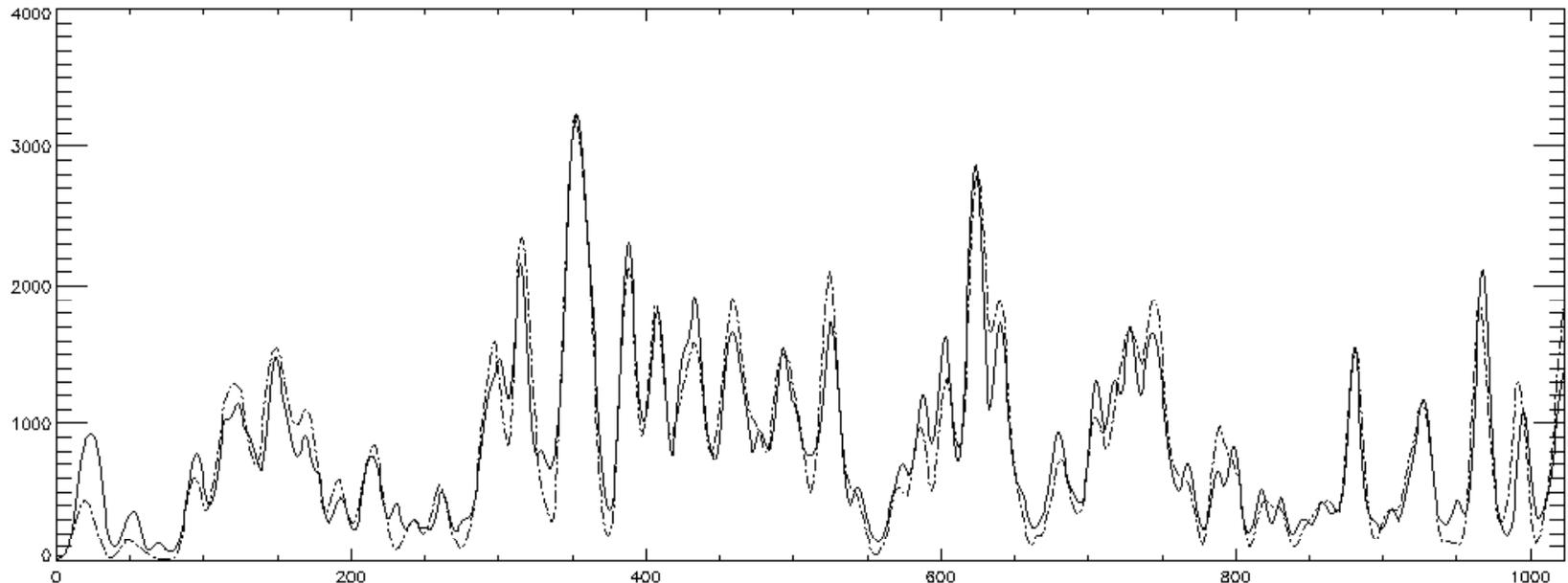
$$I_{par}(\mathbf{r}) = \int G(\mathbf{r}/z) I_{coh}(\mathbf{r} - \mathbf{r}') dr'$$

$$I_{par} = G \otimes I_{coh} \quad \text{where} \quad G = FT\{g\}$$

$$g = \frac{FT^{-1}\{I_{par}\}}{FT^{-1}\{I_{coh}\}}$$



One dimensional analysis

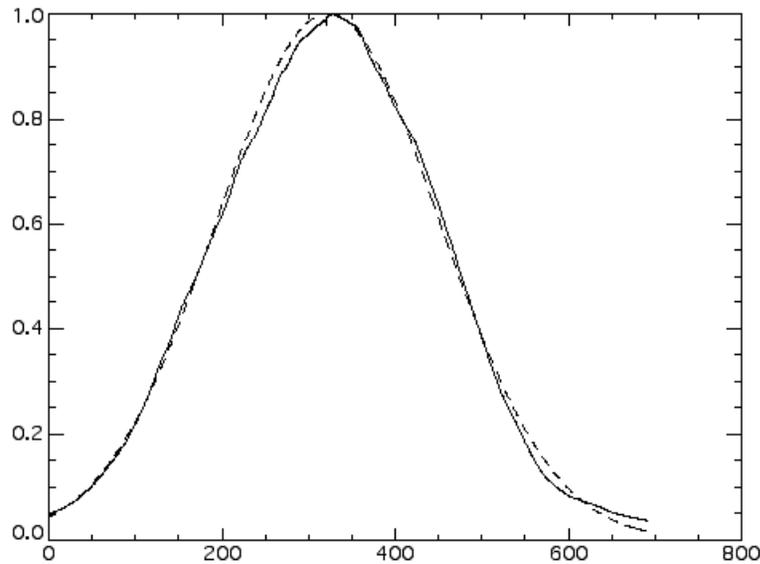


- Vertical diffraction profile collected during low emittance studies
- Energy =1500eV, diffraction distance =1.1 m, 1.21 μm thick 1D URA with 5 μm minimum slit size
- Solid line is experiment diffraction dashed line is simulation with real parameters including source size

Reduced emittance studies

High emittance

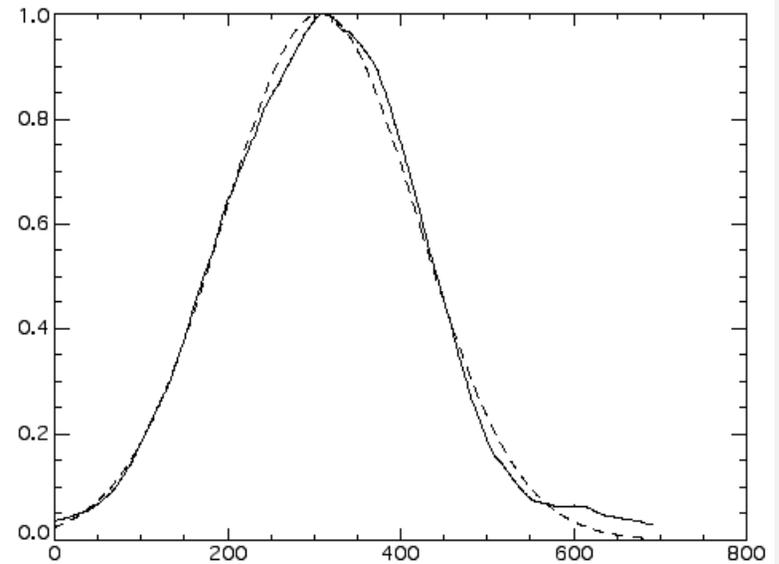
$\sigma_y = 21 \mu\text{m}$ $\sigma_{y'} = 3.9 \mu\text{rad}$
Vertical emittance = 80 pm-rad



Vertical Gaussian $\sigma = 129 \mu\text{m}$

Low emittance

$\sigma_y = 11 \mu\text{m}$ $\sigma_{y'} = 2.7 \mu\text{rad}$
Vertical emittance = 28 pm-rad



Vertical Gaussian $\sigma = 113 \mu\text{m}$

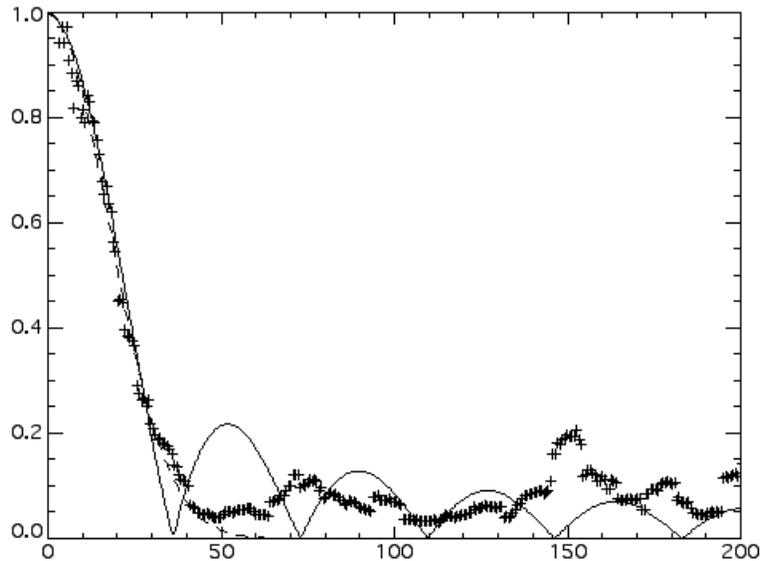
Beamline 2-ID-B, Energy = 1500 eV, source to experiment = 60.3 m

Beam profile

Reduced emittance studies

High emittance

$\sigma_y = 21 \mu\text{m}$ $\sigma_{y'} = 3.9 \mu\text{rad}$
Vertical emittance = 80 pm-rad

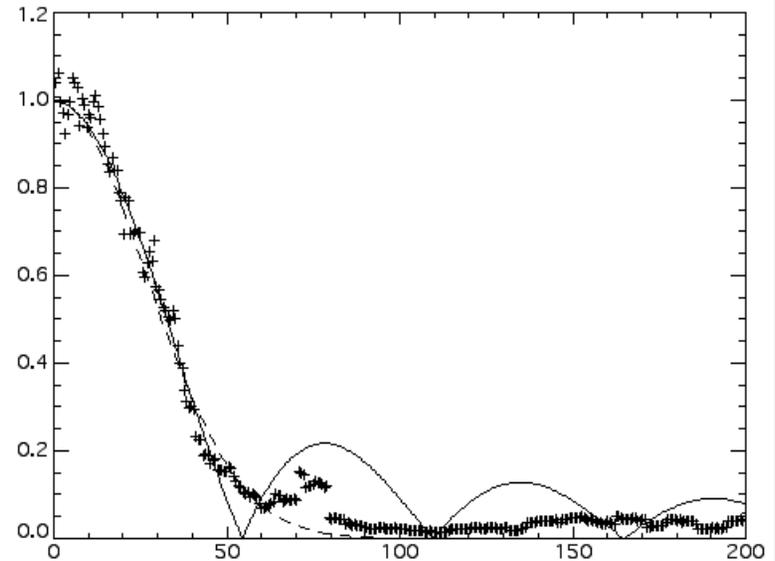


Gaussian width: $17.3 \pm 3.6 \mu\text{m}$

Source width = $180 \mu\text{m}$ at 8.0 m

Low emittance

$\sigma_y = 11 \mu\text{m}$ $\sigma_{y'} = 2.7 \mu\text{rad}$
Vertical emittance = 28 pm-rad

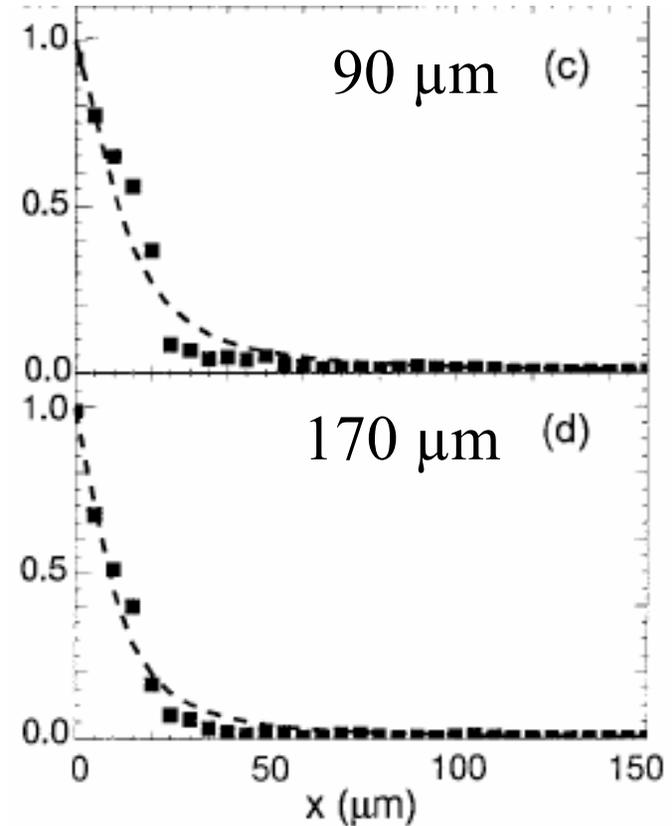
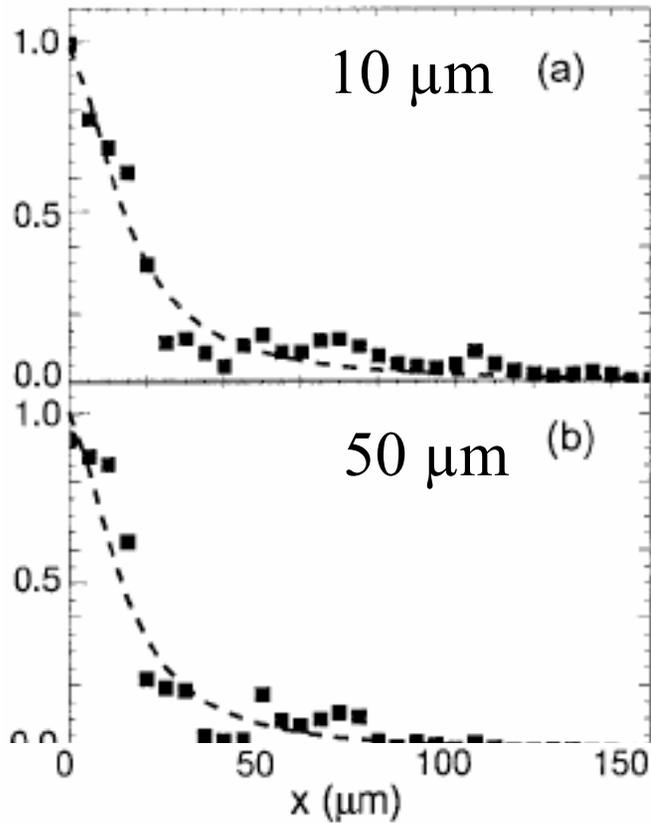


Gaussian width: $26.5 \pm 4.5 \mu\text{m}$

Source width = $120 \mu\text{m}$ at 8.0 m

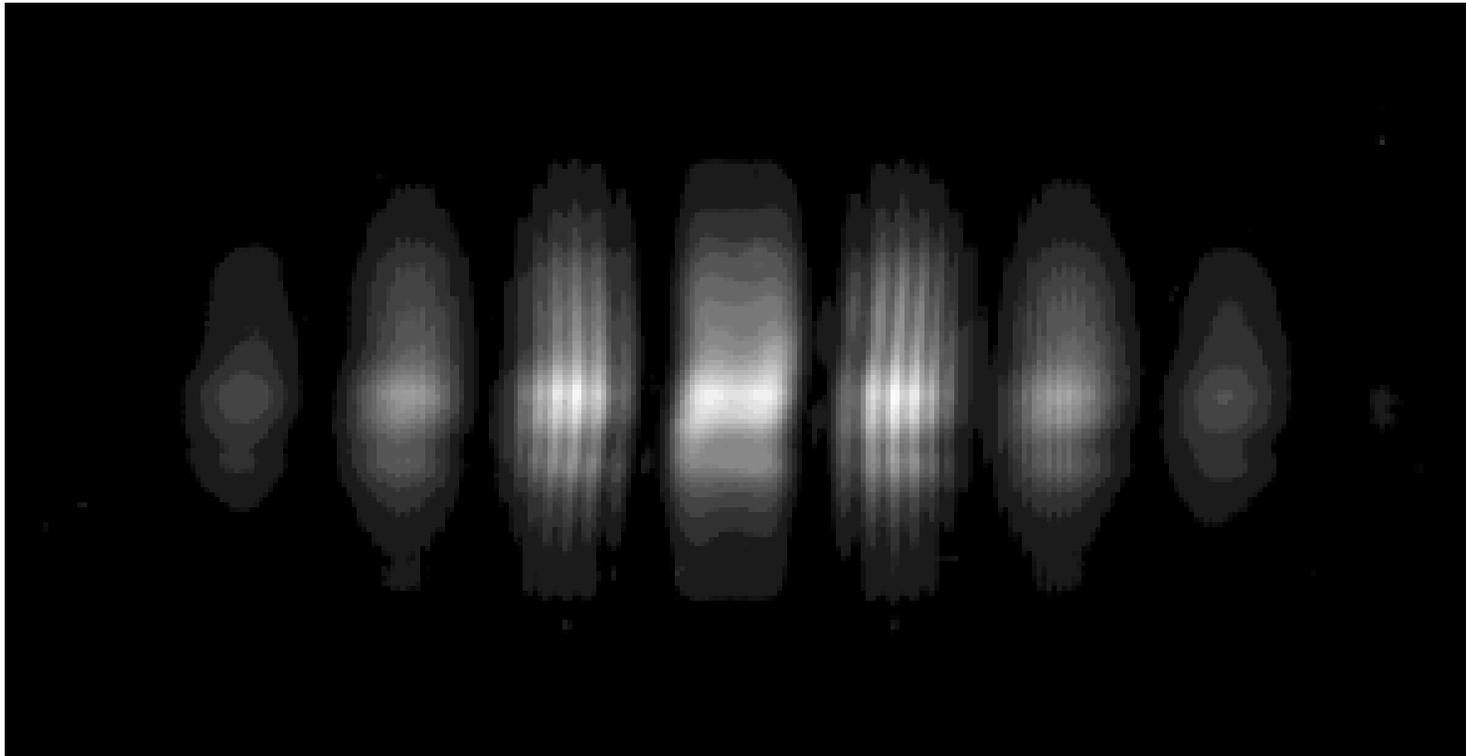
Coherence function

Spatial coherence function with phase URA



Coherence function measured at 8 keV, 43.4 m from slits of size
(a) 10 μm , (b) 50 μm , (c) 90 μm , and (d) 170 μm

Coherence "degradation"?



CCD image of Young's interference pattern with 10 μm slit separation at 1.07 m, using 1.5 keV x-rays. Image is 820 μm by 420 μm and fringe spacing is 90 μm .

Condition for full utilization of coherence by experiment: $d_{\text{aperture}} < d_{\text{speckle}}$



Summary, future work

- **Measurement of complete spatial coherence function of undulator radiation**
- **Speckle effects and coherence “degradation”**
- **Agreement with theoretical expectations**
- **URA can completely map coherence function**
- **Two dimensional measurement possible**
- **Study evolution of spatial coherence in LEUTL**
 - Measurement point after each undulator



Collaborators and acknowledgements

- **APS, X-ray Operation and Research**
 - Ian McNulty, Barry Lai, Cornelia Retsch, and Joe Arko
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 - Mike Moldovan, Ralu Divan, and Derrick Mancini
 - *Manufacture of Young's slit arrays and URAs*
- **APS, ASD**
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- **University of Melbourne, Australia**
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